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21CS42

## Fourth Semester B.E. Degree Examination, June/July 2024

## Design and Analysis of Algorithms

Time: 3 hrs.

Max. Marks: 100

*Note: Answer any FIVE full questions, choosing ONE full question from each module.*

Module-1

- 1 a. Define algorithm. Explain the following asymptotic notations:  
 i) Big On      ii) Big Omega      iii) Big Theta      (08 Marks)
- b. Design a non-recursive algorithm to find maximum element in an array of n elements. Give the Mathematical Analysis.      (08 Marks)
- c. Define time and space complexity.      (04 Marks)

OR

- 2 a. Design an algorithm for performing sequential search and compute Best, Worst and Average case efficiency.      (08 Marks)
- b. Write an algorithm to find the uniqueness of element an array and give mathematical analysis of this non recursive algorithm with steps.      (08 Marks)
- c. List and explain basic asymptotic efficiency classes.      (04 Marks)

Module-2

- 3 a. Illustrate the tracing of the Quick Sort algorithm for the following set of numbers  
 5, 3, 1, 9, 8, 2, 4, 7      (10 Marks)
- b. Apply the topological sorting algorithm for the following graph shown in Fig.Q3(b). Find the topological sequence.

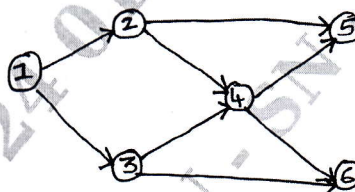


Fig.Q3(b)

(10 Marks)

OR

- 4 a. Write a C++/JAVA program for Merge Sort. Analyze its efficiency and apply the same to sort the following numbers : 4, 9, 0, -1, 6, 8, 9, 2, 3, 12.      (10 Marks)
- b. Write a recursive algorithm for Binary Search and also bring out its efficiency.      (10 Marks)

Module-3

- 5 a. Apply greedy method to obtain an optimal solution to the knapsack problem given  $M = 60$ .

$$W = \{5, 10, 20, 30, 40\}$$

$$P = \{30, 20, 100, 90, 160\}$$

Find total profit earned.

(10 Marks)

Important Note : 1. On completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages.  
 2. Any revealing of identification, appeal to evaluator and /or equations written eg,  $42+8=50$ , will be treated as malpractice.

- b. Apply single source shortest path algorithm to the following graph Fig.Q5(b). Assume vertex 'a' as source.

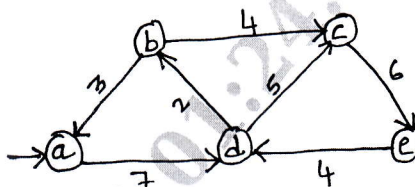


Fig.Q5(b)

(10 Marks)

OR

- 6 a. A message consisting of the character given in the table below has to be transmitted network in a secured manner.

Character	A	M	R	-
Probability	0.4	0.2	0.3	0.1

- Construct Huffman tree
  - Device Huffman codes for the given characters
  - Encode the text : RAMA\_RAMAR
  - Decode the text : 1000101
- b. Find the optimal solution using greedy for the job sequencing with dead line problem with following values:

Job	J <sub>1</sub>	J <sub>2</sub>	J <sub>3</sub>	J <sub>4</sub>	J <sub>5</sub>
Profit	10	3	33	11	40
Dead line	3	1	1	2	2

(10 Marks)

**Module-4**

- 7 a. Define a Multistage Graph. Give an example. Explain the technique of finding the minimum cost path in a multistage graph. (10 Marks)
- b. Write Floyd's Algorithm and find all pair Shortest path for the given graph. [Refer Fig.Q7(b)]

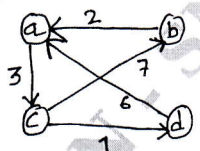


Fig.Q7(b)

(10 Marks)

OR

- 8 a. Apply the Dynamic Programming to solve travelling sales person problem for the following graph shown in Fig.Q8(a).

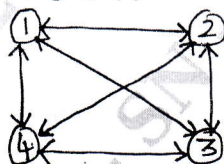


Fig.Q8(a)

C	1	2	3	4
1	0	10	15	20
2	5	0	9	10
3	6	13	0	12
4	8	8	9	0

(10 Marks)

- b. Write Horspool Algorithm for string matching. Trace the algorithm to find the pattern "ELECTION" in the text.

"EDUCATION ONLY HELPS IN SELECTION."

(10 Marks)

**Module-5**

- 9 a. Construct the state-space tree for sum of subset problem given the following data:  
 $W = \{3, 5, 6, 7\}$  and  $m = 15$ . (10 Marks)
- b. Write C++ / JAVA program to find all Hamiltonian cycles in a connected undirected Graph  $G$  of  $n$  vertices using backtracking principle. (10 Marks)

**OR**

- 10 a. Explain Branch and Bound concept. Apply Branch and Bound to the following instance of assignment problem.

	Job1	Job2	Job3	Job4
Person A	9	2	7	8
Person B	6	4	3	7
Person C	5	8	1	8
Person D	7	6	9	4

(10 Marks)

- b. Explain the following concepts :
- Graph coloring problem with an example
  - NP Complete Problem
  - NP-Hard Class Problem

(10 Marks)

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