

# CBGS Scheme

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16MDE/MMD/MST/MTP/MTR/MCM  
/MEA/CAE/MAR11

First Semester M.Tech. Degree Examination, June/July 2017

## Applied Mathematics

Time: 3 hrs.

Max. Marks: 80

Note: Answer FIVE full questions, choosing one full question from each module.

### Module-1

- 1 a. Define absolute, relative and percentage errors. An approximate value of  $\pi$  is given by  $x_1 = \frac{22}{7} = 3.1428571$  and its true value is  $x = 3.1415926$ . Find the absolute and relative errors. (05 Marks)
- b. Given  $f(x) = \sin x$ , construct the Taylor's series approximation of order 0 to 7 at  $x = \frac{\pi}{3}$ . (05 Marks)
- c. A parachutist of mass 68.1 kg jumps out of a stationary hot air balloon, use  $\frac{dv}{dt} = g - \left(\frac{C}{m}\right)v$  to compute velocity  $V$  prior to opening the chute. The drag coefficient 12.6 kg/sec. Given that  $g = 9.81 \text{ m/s}^2$ ,  $v = 0$  and  $t = 0$ . (06 Marks)

OR

- 2 a. If  $f = \frac{4x^2y^3}{z^4}$  and the error in  $x, y, z$  are 0.001. Calculate the absolute error and relative maximum error in 'f' at  $x = y = z = 1$ . (05 Marks)
- b. Find the relative error of the number  $x = 0.004997$ ,  
(i) Truncated to three decimal digits. (05 Marks)  
(ii) Rounded off to three decimal digits. (05 Marks)
- c. Find the number of terms of the exponential series such that their sum gives values of  $e^x$  at  $x = 1$  to 6 decimal places and to 8 decimal places. (06 Marks)

### Module-2

- 3 a. By using the Regula Falsi method, find an approximate root of the equation  $x^4 - x - 10 = 0$  between 1.8 and 2. Carry out three approximations. (05 Marks)
- b. Find the root of the equation  $x \log_{10} x = 1.2$  by Bisection method where the root lies between 2 and 3. Carry out four approximations. (05 Marks)
- c. Apply Newton Raphson method to find an approximate root correct to three decimal places, of the equation  $xe^x = 2$ . (06 Marks)

OR

- 4 a. Find the root of the equation  $f(x) = x^3 - 2x - 5 = 0$  in (2, 3) by Muller's method. (08 Marks)
- b. Find the real root of the equation  $x^3 - 6x^2 + 11x - 6 = 0$  by Graeffe's root squaring method. (08 Marks)

### Module-3

- 5 a. Evaluate  $\int_0^6 \frac{dx}{1+x^2}$  by using,  
(i) Trapezoidal rule. (ii) Simpson's  $\frac{1}{3}$  rule with  $h = 1$ . (08 Marks)
- b. Use Romberg's method to compute  $\int_0^1 \frac{1}{1+x} dx$ , correct to three decimal places. (08 Marks)

1 of 3

OR

- 6 a. Given :

x	1.0	1.2	1.4	1.6	1.8	2.0
y	2.72	3.32	4.06	4.96	6.05	7.39

Find  $y'$  and  $y''$  at  $x = 1.2$ 

(08 Marks)

- b. The following table gives the temperature
- $\theta$
- (in degree Celsius) of a cooling body at different instant of time
- $t$
- (in seconds)

t	1	3	5	7	9
$\theta$	85.3	74.5	67	60.5	54.3

Find approximately rate of cooling at  $t = 8$  seconds.

(08 Marks)

**Module-4**

- 7 a. Solve the system of equations by Gauss elimination method,

$$2x_1 - x_2 + 3x_3 = 1$$

$$-3x_1 + 4x_2 - 5x_3 = 0$$

$$x_1 + 3x_2 - 6x_3 = 0$$

(05 Marks)

- b. Find the inverse of a matrix
- $\begin{bmatrix} 1 & 1 & 3 \\ 0 & 2 & -6 \\ 0 & -2 & 2 \end{bmatrix}$
- by Gauss Jordan method.

(05 Marks)

- c. Solve, by Jacobi iterative method, the equations
- $20x + y - 2z = 17$
- ,
- $3x + 20y - z = -18$
- ,
- $2x - 3y + 20z = 25$
- .

(06 Marks)

OR

- 8 a. By using Given's method find the eigen values of the tridiagonal matrix
- $\begin{bmatrix} 2 & -1 & 0 \\ -1 & 2 & -1 \\ 0 & -1 & 2 \end{bmatrix}$
- .

(08 Marks)

- b. Using the Jacobi method find all the eigen values and the corresponding eigenvectors of the

matrix,  $\begin{bmatrix} 1 & \sqrt{2} & 2 \\ \sqrt{2} & 3 & \sqrt{2} \\ 2 & \sqrt{2} & 1 \end{bmatrix}$ .

(08 Marks)

**Module-5**

- 9 a. Show that
- $\{v_1, v_2, v_3\}$
- is an orthogonal basis of
- $R^3$
- , where
- $V_1 = \left[ \frac{3}{\sqrt{11}}, \frac{1}{\sqrt{11}}, \frac{1}{\sqrt{11}} \right]^T$
- ,

$$V_2 = \left[ \frac{-1}{\sqrt{6}}, \frac{2}{\sqrt{6}}, \frac{1}{\sqrt{6}} \right]^T, V_3 = \left[ \frac{-1}{\sqrt{66}}, \frac{-4}{\sqrt{66}}, \frac{7}{\sqrt{66}} \right]^T.$$

(05 Marks)

- b. Let
- $y = \begin{bmatrix} 7 \\ 6 \end{bmatrix}$
- and
- $u = \begin{bmatrix} 4 \\ 2 \end{bmatrix}$
- . Find the orthogonal projection of
- $y$
- onto
- $u$
- .

(05 Marks)

- c. Show that
- $S = \{u_1, u_2, u_3\}$
- is an orthogonal set. Express the vector
- $y = [6, 1, -8]^T$
- as a linear

combination of the vectors in  $S$  where  $u_1 = \begin{bmatrix} 3 \\ 1 \\ 1 \end{bmatrix}$ ,  $u_2 = \begin{bmatrix} -1 \\ 2 \\ 1 \end{bmatrix}$ ,  $u_3 = \begin{bmatrix} -1 \\ 2 \\ 7 \\ 2 \end{bmatrix}$ .

(06 Marks)

June/July 2017

16MDE/MMD/MST/MTP/MTR/MCM/MEA/CAE/MAR11

OR

- 10 a. Find a QR factorization of,  $A = \begin{bmatrix} 1 & 0 & 0 \\ 1 & 1 & 0 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix}$ . (08 Marks)

- b. Find a least square solution of  $AX = b$  for,

$$A = \begin{bmatrix} 1 & 1 & 0 & 0 \\ 1 & 1 & 0 & 0 \\ 1 & 0 & 1 & 0 \\ 1 & 0 & 1 & 0 \\ 1 & 0 & 0 & 1 \\ 1 & 0 & 0 & 1 \end{bmatrix}, b = \begin{bmatrix} -3 \\ -1 \\ 0 \\ 2 \\ 5 \\ 1 \end{bmatrix}$$

(08 Marks)

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