

CBCS Scheme

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16MDE/MMD/MST/MTP/MTR/
MCM/MEA/CAE/MAR/MAU11

First Semester M.Tech. Degree Examination, Dec.2016/Jan.2017

Applied Mathematics

Time: 3 hrs.

Max. Marks: 80

Note: Answer any FIVE full questions, choosing one full question from each module.

Module-1

- 1 a. Explain in brief :
 - i) Significant figures
 - ii) Truncation errors
 - iii) Rounding off
 - iv) Percentage errors. (08 Marks)
- b. Establish a simple mathematical model for a falling body (parachutist) as $\frac{dv}{dt} = g - \left(\frac{c}{m}\right)v$ and obtain its solution as $v(t) = \frac{mg}{c} \left[1 - e^{-\left(\frac{c}{m}\right)t} \right]$ with m-mass of the falling body, C-the drag coefficient g-gravitational force, v-velocity and t-time. (08 Marks)

OR

- 2 a. Round off the numbers 865250 and 37.46235 to four significant figures and compute
 - i) absolute error
 - ii) relative error and
 - iii) percentage error. (08 Marks)
- b. Find graphically an approximate value of the root of the equation $3 - x = e^{x-1}$. (08 Marks)

Module-2

- 3 a. Explain Regula-Falsi method to find the root of the equation $f(x) = 0$ with suitable formulation. Use it to find the root of the equation $x \log_{10} x = 1.2$ to four decimal places with three approximations. (08 Marks)
- b. With suitable formulation explain Newton Raphson method to find the root of the equation $f(x) = 0$. Use it to find the root of $3x = \cos x + 1$ with initial value as 0.6 (take two approximations). (08 Marks)

OR

- 4 a. Explain the necessary steps involved in Muller's method to find the root of the equation $f(x) = 0$. Use it to find the first approximation of $\cos x = xe^x$ which lies between $[0, 1]$. (08 Marks)
- b. Use Graeffe's root squaring method by squaring thrice from the equation $x^3 - 2x^2 - 5x + 6 = 0$. (08 Marks)

Important Note : 1. On completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages.
2. Any revealing of identification, appeal to evaluator and /or equations written eg. $42+8=50$, will be treated as malpractice.

Module-3

- 5 a. State equations for $\frac{dy}{dx}$ and $\frac{d^2y}{dx^2}$ in the case of numerical differentiation on forward and backward differences. Find $\frac{dy}{dx}$ and $\frac{d^2y}{dx^2}$ at $x = 1.5$ given the following table (08 Marks)
- | x | 1.0 | 1.5 | 2.0 | 2.5 | 3.0 |
|----------|-------|-------|-------|-------|-------|
| y = f(x) | 1.729 | 1.691 | 1.505 | 1.416 | 1.311 |

- b. Starting from general quadrature formula (Newton – Cote's formula) establish Wedde's formula using numerical integration. Use it to find $\int_4^{5.2} \log_e x \, dx$ with 7 ordinates. (08 Marks)

OR

- 6 a. Apply Cramer's rule to solve the equations
 $3x + y + 2z = 3$
 $2x - 3y - z = -3$
 $x - 2y + z = 4$ (08 Marks)
- b. Apply Gauss – Jordan method to solve the equations
 $x + y + z = 9$
 $2x - 3y + 4z = 13$
 $3x + 4y + 5z = 40$. (08 Marks)

Module-4

- 7 a. Use Cholesky's method to solve the equations (08 Marks)
 $2x + 3y + z = 9$
 $x + 2y + 3z = 6$
 $3x + y + 2z = 8$
- b. Solve the following equations by Jacobi's iteration method. (Use 4 iterations). (08 Marks)
 $20x + y - 2z = 17$
 $3x + 20y - z = -18$
 $2x - 3y + 20z = 25$
 Take initial values as $x_0 = y_0 = z_0 = 0$.

OR

- 8 a. Determine the largest Eigen value and the corresponding Eigen vector of the matrix with 5 (five) iterations given that,
 $A = \begin{bmatrix} 2 & -1 & 0 \\ -1 & 2 & -1 \\ 0 & -1 & 2 \end{bmatrix}$ Take the initial vector as $[1 \ 0 \ 0]^T$. (08 Marks)
- b. Use House – holder's method to reduce the following matrix to the tri-diagonal form.
 $A = \begin{bmatrix} 1 & 4 & 3 \\ 4 & 1 & 2 \\ 3 & 2 & 1 \end{bmatrix}$ (08 Marks)

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Module-5

- 9 a. Give the properties of linear transformation. The columns of $I_2 = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$ are denoted by

$e_1 = \begin{bmatrix} 1 \\ 0 \end{bmatrix}$, $e_2 = \begin{bmatrix} 0 \\ 1 \end{bmatrix}$, suppose T is a linear transformation from R^2 to R^3 such that

$T(e_1) = \begin{bmatrix} 5 \\ -7 \\ 2 \end{bmatrix}$ and $T(e_2) = \begin{bmatrix} -3 \\ 8 \\ 0 \end{bmatrix}$, find the image of an arbitrary X in R^2 . (08 Marks)

- b. If $T : R^n \rightarrow R^m$ be a linear transformation, prove that

- T is one - to - one if and only if the equation $T(X) = 0$ has a trivial solution.
- T maps R^n onto R^m if and only if the columns of A span R^m .
- T is one - to - one if and only if the columns of A are linearly independent.

(08 Marks)

OR

- 10 a. Give a geometrical interpretation of orthogonal projection.

If $u_1 = \begin{bmatrix} 2 \\ 5 \\ -1 \end{bmatrix}$, $u_2 = \begin{bmatrix} -2 \\ 1 \\ 1 \end{bmatrix}$, $y = \begin{bmatrix} 1 \\ 2 \\ 3 \end{bmatrix}$ and $\{u_1, u_2\}$ is an orthogonal basis for $w = \text{span} \{u_1, u_2\}$,

write y as the sum of vector in w and a vector orthogonal to w . (08 Marks)

- b. Discuss in brief :

- Gram - Schmidt process
- Least square lines
- The general linear model.

(08 Marks)
