

First Semester M.Tech. Degree Examination, Dec.2023/Jan.2024 Applied Mathematics

Time: 3 hrs.

Max. Marks: 100

Note: 1. Answer any FIVE full questions, choosing ONE full question from each module.

2. M : Marks , L: Bloom's level , C: Course outcomes.

Module – 1				M	L	C
Q.1	a.	Solve the system of equations $4x + 10y + 8z = 44$, $10x + 26y + 26z = 128$, $8x + 26y + 61z = 214$ using Cholesky method.		10	L3	CO1
	b.	Find the inverse of the matrix using partition method, $\begin{bmatrix} 1 & 1 & 1 \\ 4 & 3 & -1 \\ 3 & 5 & 3 \end{bmatrix}$		10	L3	CO1
OR						
Q.2	a.	Solve the system of equation : $x_1 + x_2 + x_3 = 1$, $4x_1 + 3x_2 - x_3 = 6$, $3x_1 + 5x_2 + 3x_3 = 4$ by triangulisation method.		10	L3	CO1
	b.	Apply Gauss Seidel iterative method to solve the system of equations, $10x_1 - 2x_2 - x_3 - x_4 = 3$, $-2x_1 + 10x_2 - x_3 - x_4 = 15$, $-x_1 - x_2 + 10x_3 - 2x_4 = 27$, $-x_1 - x_2 - 2x_3 + 10x_4 = -9$		10	L3	CO1
Module – 2						
Q.3	a.	Find the matrix of the linear transformation $T : V_3(R) \rightarrow V_2(R)$ defined by $T(x, y, z) = (x + y, y + z)$.		10	L2	CO2
	b.	Consider $f(t) = 3t - 5$ and $g(t) = t^2$ in the polynomial space $P(t)$ with inner product $\langle f, g \rangle = \int_0^1 f(t)g(t).dt$. (i) Find $\langle f, g \rangle$ (ii) Find $\ f\ $ and $\ g\ $		10	L2	CO2
OR						
Q.4	a.	Consider the subspace U of $\mathbb{R}^4$ spanned by the vectors $V_1 = (1, 1, 1, 1)$, $V_2 = (1, 1, 2, 4)$, $V_3 = (1, 2, -4, -3)$ Find (i) Orthogonal basis of U (ii) an orthonormal basis of U by applying Gram-Schmidt orthogonalization.		10	L2	CO2

	b.	Find the least square solution of $AX = B$ for, $A = \begin{bmatrix} 1 & 3 & 5 \\ 1 & 1 & 0 \\ 1 & 1 & 2 \\ 1 & 3 & 3 \end{bmatrix}, B = \begin{bmatrix} 3 \\ 5 \\ 7 \\ -3 \end{bmatrix}$	10	L2	CO2														
Module – 3																			
Q.5	a.	Diagonalize the matrix, $A = \begin{bmatrix} 8 & -6 & 2 \\ -6 & 7 & -4 \\ 2 & -4 & 3 \end{bmatrix}$.	10	L3	CO3														
	b.	Find the largest eigen value and the eigen vector of the matrix, $\begin{bmatrix} 2 & 0 & 1 \\ 0 & 2 & 0 \\ 1 & 0 & 2 \end{bmatrix}$ by power method.	10	L3	CO3														
OR																			
Q.6	a.	Solve by Jacobi method, $\begin{bmatrix} 2 & \sqrt{2} & 4 \\ \sqrt{2} & 6 & \sqrt{2} \\ 4 & \sqrt{2} & 2 \end{bmatrix}$.	10	L3	CO3														
	b.	Find singular value decomposition of a matrix, $A = \begin{bmatrix} 1 & 1 \\ 0 & 1 \\ -1 & 1 \end{bmatrix}$.	10	L3	CO3														
Module – 4																			
Q.7	a.	Define : (i) Random sampling (ii) Sampling distribution (iii) Statistical hypothesis (iv) Null hypothesis (v) Level of significance.	10	L2	CO4														
	b.	Five dice are thrown 96 times and numbers 1, 2 or 3 appearing on the face of the dice follows the frequency distribution as follows : <table border="1"><tr><td>No. of dice shown 1, 2 or 3</td><td>5</td><td>4</td><td>3</td><td>2</td><td>1</td><td>0</td></tr><tr><td>Frequency</td><td>7</td><td>19</td><td>35</td><td>24</td><td>8</td><td>3</td></tr></table> Test the hypothesis that the data follows a binomial distribution, ($\chi^2_{0.05} = 11.07$ for 5 degree of freedom) .	No. of dice shown 1, 2 or 3	5	4	3	2	1	0	Frequency	7	19	35	24	8	3	10	L2	CO4
No. of dice shown 1, 2 or 3	5	4	3	2	1	0													
Frequency	7	19	35	24	8	3													
OR																			
Q.8	a.	A certain stimulus administered to each of 12 patients resulted in the following increases of blood pressure 5, 2, 8, -1, 3, 0, -2, 1, 5, 0, 4, 6. Can it be concluded that the stimulus will increase the blood pressure? (Table value : $t_{0.05}$ for 11 degree of freedom = 2.201)	10	L2	CO4														