

First Semester M.Tech. Degree Examination, Dec.2023/Jan.2024

Digital Circuits and Logic Design

Time: 3 hrs.

Max. Marks: 100

Note: 1. Answer any FIVE full questions, choosing ONE full question from each module.
2. M : Marks, L: Bloom's level, C: Course outcomes.

Module - 1			M	L	C
Q.1	a.	Explain the different properties of threshold logic.	6	L2	CO1
	b.	Identify and realize the threshold function $f = x_1x_2\bar{x}_3x_4 + x_2\bar{x}_3\bar{x}_4$	10	L3	CO2
	c.	Explain the capabilities of Threshold logic.	4	L2	CO1
OR					
Q.2	a.	Determine which of the following function is unate or not i) $F_1(x_1, x_2, x_3, x_4) = \Sigma(1, 2, 3, 8, 9, 10, 11, 12, 14)$ ii) $F_2(x_1, x_2, x_3, x_4) = \Sigma(0, 8, 9, 10, 11, 12, 13, 14)$ iii) $F_3(x_1, x_2, x_3, x_4) = \Sigma(2, 3, 6, 10, 11, 12, 14, 15)$	10	L3	CO2
	b.	Determine whether following functions are threshold or not i) $F_1(x_1, x_2, x_3) = \Sigma(0, 2, 4, 5, 6)$ ii) $F_2(x_1, x_2, x_3) = \Sigma(0, 3, 5, 6)$ If the given functions are the threshold, then write down the threshold gate.	10	L3	CO2
Module - 2					
Q.3	a.	Using path sensitization method, derive the test vector for the s - a - 0 and s - a - 1 faults at 'g' and 'h' in the circuit shown in Fig Q3(a)	10	L3	CO4
	b.	Use the map method to find a minimal set of tests for multiple faults for the 2-level AND-OR realization of the function : $F(w, x, y, z) = w\bar{z} + x\bar{y} + \bar{w}x + w\bar{x}y$.	10	L3	CO4
OR					
Q.4	a.	For the circuit shown in Fig Q4(a), find all the tests to detect the faults x_3 s - a - 0 and x_3 s - a - 1.	10	L3	CO4

	b.	Use the map method to find a minimal set of test for multiple faults for the 2-levels OR-AND realization of the function : $F(w, x, y, z) = (w + \bar{x})(x + \bar{z})(\bar{w} + y + \bar{z})$.	10	L3	CO4																																																															
Module – 3																																																																				
Q.5	a.	What is merger graph? Draw the merger graph and reduced graph for the machine given in Table Q5(a). <table><tr><th rowspan="2">PS</th><th colspan="4">NS, Z</th></tr><tr><th>I₁</th><th>I₂</th><th>I₃</th><th>I₄</th></tr><tr><td>A</td><td>–</td><td>E, 1</td><td>B, 1</td><td>–</td></tr><tr><td>B</td><td>–</td><td>D, 1</td><td>–</td><td>F, 1</td></tr><tr><td>C</td><td>F, 1</td><td>–</td><td>–</td><td>–</td></tr><tr><td>D</td><td>–</td><td>–</td><td>C, 1</td><td>–</td></tr><tr><td>E</td><td>C, 0</td><td>–</td><td>A, 0</td><td>F, 1</td></tr><tr><td>F</td><td>D, 0</td><td>A, 1</td><td>B, 0</td><td>–</td></tr></table> Table Q5(a)	PS	NS, Z				I ₁	I ₂	I ₃	I ₄	A	–	E, 1	B, 1	–	B	–	D, 1	–	F, 1	C	F, 1	–	–	–	D	–	–	C, 1	–	E	C, 0	–	A, 0	F, 1	F	D, 0	A, 1	B, 0	–	10	L3	CO2																								
PS	NS, Z																																																																			
	I ₁	I ₂	I ₃	I ₄																																																																
A	–	E, 1	B, 1	–																																																																
B	–	D, 1	–	F, 1																																																																
C	F, 1	–	–	–																																																																
D	–	–	C, 1	–																																																																
E	C, 0	–	A, 0	F, 1																																																																
F	D, 0	A, 1	B, 0	–																																																																
	b.	Prove that the machine shown in Table Q5(b) is minimal. Also draw the compatibility graph. <table><tr><th rowspan="2">PS</th><th colspan="7">NS, Z</th></tr><tr><th>I₁</th><th>I₂</th><th>I₃</th><th>I₄</th><th>I₅</th><th>I₆</th><th>I₇</th></tr><tr><td>A</td><td>F, 0</td><td>A, –</td><td>D, –</td><td>C, –</td><td>–</td><td>–</td><td>–</td></tr><tr><td>B</td><td>–, 1</td><td>–</td><td>–</td><td>–</td><td>C, –</td><td>D, –</td><td>E, –</td></tr><tr><td>C</td><td>C, –</td><td>E, –</td><td>–</td><td>–</td><td>F, 0</td><td>B, –</td><td>–</td></tr><tr><td>D</td><td>–</td><td>–</td><td>F, –</td><td>E, –</td><td>–, 1</td><td>–</td><td>A, –</td></tr><tr><td>E</td><td>A, –</td><td>–</td><td>A, 1</td><td>–</td><td>B, –</td><td>–</td><td>C, –</td></tr><tr><td>F</td><td>–</td><td>D, –</td><td>–, 0</td><td>B, –</td><td>–</td><td>E, –</td><td>–</td></tr></table> Table Q5(b)	PS	NS, Z							I ₁	I ₂	I ₃	I ₄	I ₅	I ₆	I ₇	A	F, 0	A, –	D, –	C, –	–	–	–	B	–, 1	–	–	–	C, –	D, –	E, –	C	C, –	E, –	–	–	F, 0	B, –	–	D	–	–	F, –	E, –	–, 1	–	A, –	E	A, –	–	A, 1	–	B, –	–	C, –	F	–	D, –	–, 0	B, –	–	E, –	–	10	L3	CO2
PS	NS, Z																																																																			
	I ₁	I ₂	I ₃	I ₄	I ₅	I ₆	I ₇																																																													
A	F, 0	A, –	D, –	C, –	–	–	–																																																													
B	–, 1	–	–	–	C, –	D, –	E, –																																																													
C	C, –	E, –	–	–	F, 0	B, –	–																																																													
D	–	–	F, –	E, –	–, 1	–	A, –																																																													
E	A, –	–	A, 1	–	B, –	–	C, –																																																													
F	–	D, –	–, 0	B, –	–	E, –	–																																																													
OR																																																																				
Q.6	a.	Explain different types of fault location experiments with example.	10	L3	CO2																																																															
	b.	Explain the present type of fault location experiment by considering fault table as shown in table Q6(b). Write down corresponding i) Reduced table ii) Fault dictionary. Also find out different sets of faults. <table><tr><th></th><th>F₁</th><th>F₂</th><th>F₃</th><th>F₄</th><th>F₅</th><th>F₆</th></tr><tr><td>T₁</td><td></td><td></td><td></td><td></td><td>1</td><td>1</td></tr><tr><td>T₂</td><td>1</td><td></td><td>1</td><td></td><td>1</td><td></td></tr><tr><td>T₃</td><td></td><td></td><td></td><td>1</td><td>1</td><td></td></tr><tr><td>T₄</td><td></td><td>1</td><td>1</td><td></td><td></td><td></td></tr><tr><td>T₅</td><td>1</td><td></td><td></td><td></td><td></td><td>1</td></tr><tr><td>T₆</td><td>1</td><td></td><td>1</td><td></td><td></td><td>1</td></tr></table> Table Q6(b)		F ₁	F ₂	F ₃	F ₄	F ₅	F ₆	T ₁					1	1	T ₂	1		1		1		T ₃				1	1		T ₄		1	1				T ₅	1					1	T ₆	1		1			1	10	L3	CO4														
	F ₁	F ₂	F ₃	F ₄	F ₅	F ₆																																																														
T ₁					1	1																																																														
T ₂	1		1		1																																																															
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T ₅	1					1																																																														
T ₆	1		1			1																																																														
Module – 4																																																																				
Q.7	a.	For the machine given in Table Q7(a), give the circuit diagram and two possible state assignments with their logical equations. <table><tr><th rowspan="2">PS</th><th colspan="2">NS</th><th colspan="2">Z</th></tr><tr><th>Z = 0</th><th>Z = 1</th><th>Z = 0</th><th>Z = 1</th></tr><tr><td>A</td><td>A</td><td>D</td><td>0</td><td>1</td></tr><tr><td>B</td><td>A</td><td>C</td><td>0</td><td>0</td></tr><tr><td>C</td><td>C</td><td>B</td><td>0</td><td>0</td></tr><tr><td>D</td><td>C</td><td>A</td><td>0</td><td>1</td></tr></table> Fig Q7(a)	PS	NS		Z		Z = 0	Z = 1	Z = 0	Z = 1	A	A	D	0	1	B	A	C	0	0	C	C	B	0	0	D	C	A	0	1	10	L3	CO2																																		
PS	NS			Z																																																																
	Z = 0	Z = 1	Z = 0	Z = 1																																																																
A	A	D	0	1																																																																
B	A	C	0	0																																																																
C	C	B	0	0																																																																
D	C	A	0	1																																																																

	b. For the machine shown in Fig Q7(b), list all closed partitions by considering input and outputs consistent partitions : $\lambda_i = \{A, E, F ; B, C, D, G\}$ $\lambda_o = \{A, E, F ; B, D ; C, G\}$ <table><tr><th rowspan="2">PS</th><th colspan="2">NS</th><th colspan="2">Z</th></tr><tr><th>X = 0</th><th>X = 1</th><th>X = 0</th><th>X = 1</th></tr><tr><td>A</td><td>B</td><td>C</td><td>0</td><td>0</td></tr><tr><td>B</td><td>A</td><td>F</td><td>1</td><td>1</td></tr><tr><td>C</td><td>F</td><td>E</td><td>1</td><td>0</td></tr><tr><td>D</td><td>F</td><td>E</td><td>1</td><td>1</td></tr><tr><td>E</td><td>G</td><td>D</td><td>0</td><td>0</td></tr><tr><td>F</td><td>D</td><td>B</td><td>0</td><td>0</td></tr><tr><td>G</td><td>E</td><td>F</td><td>1</td><td>0</td></tr></table> Table Q7(b)	PS	NS		Z		X = 0	X = 1	X = 0	X = 1	A	B	C	0	0	B	A	F	1	1	C	F	E	1	0	D	F	E	1	1	E	G	D	0	0	F	D	B	0	0	G	E	F	1	0	10	L3	CO4
PS	NS		Z																																													
	X = 0	X = 1	X = 0	X = 1																																												
A	B	C	0	0																																												
B	A	F	1	1																																												
C	F	E	1	0																																												
D	F	E	1	1																																												
E	G	D	0	0																																												
F	D	B	0	0																																												
G	E	F	1	0																																												
OR																																																
Q.8	a. For the machine given in Table Q8(a). Find : i) Closed partition ii) Give the functional relationship based on the $r_1 = \{A, B, C, D ; E, F, G, H\}$ $r_2 = \lambda_o = \{A, C, E, G ; B, D, F, H\}$ iii) Write down the Schematic diagrams π – lattice for machine given in Table Q8(a) <table><tr><th rowspan="2">PS</th><th colspan="2">NS</th><th rowspan="2">Z</th></tr><tr><th>X = 0</th><th>X = 1</th></tr><tr><td>A</td><td>G</td><td>D</td><td>1</td></tr><tr><td>B</td><td>H</td><td>C</td><td>0</td></tr><tr><td>C</td><td>F</td><td>G</td><td>1</td></tr><tr><td>D</td><td>E</td><td>G</td><td>0</td></tr><tr><td>E</td><td>C</td><td>B</td><td>1</td></tr><tr><td>F</td><td>C</td><td>A</td><td>0</td></tr><tr><td>G</td><td>A</td><td>E</td><td>1</td></tr><tr><td>H</td><td>B</td><td>F</td><td>0</td></tr></table> Table Q8(a)	PS	NS		Z	X = 0	X = 1	A	G	D	1	B	H	C	0	C	F	G	1	D	E	G	0	E	C	B	1	F	C	A	0	G	A	E	1	H	B	F	0	10	L3	CO4						
PS	NS		Z																																													
	X = 0	X = 1																																														
A	G	D	1																																													
B	H	C	0																																													
C	F	G	1																																													
D	E	G	0																																													
E	C	B	1																																													
F	C	A	0																																													
G	A	E	1																																													
H	B	F	0																																													
	b. For the machine shown in Table Q8(b), determine the π-lattice and basic partitions. <table><tr><th rowspan="2">PS</th><th colspan="2">NS</th></tr><tr><th>X = 0</th><th>X = 1</th></tr><tr><td>A</td><td>E</td><td>B</td></tr><tr><td>B</td><td>E</td><td>A</td></tr><tr><td>C</td><td>D</td><td>A</td></tr><tr><td>D</td><td>C</td><td>F</td></tr><tr><td>E</td><td>F</td><td>C</td></tr><tr><td>F</td><td>E</td><td>C</td></tr></table> Table Q8(b)	PS	NS		X = 0	X = 1	A	E	B	B	E	A	C	D	A	D	C	F	E	F	C	F	E	C	10	L3	CO4																					
PS	NS																																															
	X = 0	X = 1																																														
A	E	B																																														
B	E	A																																														
C	D	A																																														
D	C	F																																														
E	F	C																																														
F	E	C																																														
Module – 5																																																
Q.9	a. Explain synchronizing experiments. Find the shortest sequence for the machine given in Table Q9(a)	10	L3	CO5																																												

		<table><tr><th rowspan="2">PS</th><th colspan="2">NS, Z</th></tr><tr><th>X = 0</th><th>X = 1</th></tr><tr><td>A</td><td>B, 0</td><td>D, 0</td></tr><tr><td>B</td><td>A, 0</td><td>B, 0</td></tr><tr><td>C</td><td>D, 1</td><td>A, 0</td></tr><tr><td>D</td><td>D, 1</td><td>C, 0</td></tr></table> Table Q9(a)	PS	NS, Z		X = 0	X = 1	A	B, 0	D, 0	B	A, 0	B, 0	C	D, 1	A, 0	D	D, 1	C, 0													
PS	NS, Z																															
	X = 0	X = 1																														
A	B, 0	D, 0																														
B	A, 0	B, 0																														
C	D, 1	A, 0																														
D	D, 1	C, 0																														
	b.	Explain the second algorithm by taking the examples of machine given in Table Q9(b).	10	L3	CO5																											
		<table><tr><th rowspan="2">PS</th><th colspan="2">NS, Z</th></tr><tr><th>X = 0</th><th>X = 1</th></tr><tr><td>A</td><td>B, 01</td><td>D, 00</td></tr><tr><td>B</td><td>A, 00</td><td>B, 00</td></tr><tr><td>C</td><td>D, 10</td><td>A, 01</td></tr><tr><td>D</td><td>D, 11</td><td>C, 01</td></tr></table> Table Q9(b)	PS	NS, Z		X = 0	X = 1	A	B, 01	D, 00	B	A, 00	B, 00	C	D, 10	A, 01	D	D, 11	C, 01													
PS	NS, Z																															
	X = 0	X = 1																														
A	B, 01	D, 00																														
B	A, 00	B, 00																														
C	D, 10	A, 01																														
D	D, 11	C, 01																														
OR																																
Q.10	a.	Find the shortest Homing sequence and the shortest synchronizing sequence for the machining given in Table Q10(a)	10	L3	CO5																											
		<table><tr><th rowspan="2">PS</th><th colspan="2">NS,Z</th></tr><tr><th>X = 0</th><th>X = 1</th></tr><tr><td>A</td><td>A, 1</td><td>E, 0</td></tr><tr><td>B</td><td>A, 0</td><td>C, 0</td></tr><tr><td>C</td><td>B, 0</td><td>D, 1</td></tr><tr><td>D</td><td>C, 1</td><td>C, 0</td></tr><tr><td>E</td><td>C, 0</td><td>D, 0</td></tr></table> Table Q10(a)	PS	NS,Z		X = 0	X = 1	A	A, 1	E, 0	B	A, 0	C, 0	C	B, 0	D, 1	D	C, 1	C, 0	E	C, 0	D, 0										
PS	NS,Z																															
	X = 0	X = 1																														
A	A, 1	E, 0																														
B	A, 0	C, 0																														
C	B, 0	D, 1																														
D	C, 1	C, 0																														
E	C, 0	D, 0																														
	b.	Explain the different steps involving in machine identification with the help of following data :	10	L3	CO5																											
		<table><tr><td>Time</td><td>:</td><td>t₁ – t₂</td><td>t₂ – t₃</td><td>t₃ – t₄</td><td>t₄ – t₅</td><td>t₅ – t₆</td><td>t₆ – t₇</td><td>t₇ – t₈</td></tr><tr><td>Input</td><td>:</td><td>1</td><td>1</td><td>1</td><td>0</td><td>1</td><td>0</td><td>1</td></tr><tr><td>Output</td><td>:</td><td>0</td><td>1</td><td>0</td><td>0</td><td>1</td><td>0</td><td>0</td></tr></table>	Time	:	t ₁ – t ₂	t ₂ – t ₃	t ₃ – t ₄	t ₄ – t ₅	t ₅ – t ₆	t ₆ – t ₇	t ₇ – t ₈	Input	:	1	1	1	0	1	0	1	Output	:	0	1	0	0	1	0	0			
Time	:	t ₁ – t ₂	t ₂ – t ₃	t ₃ – t ₄	t ₄ – t ₅	t ₅ – t ₆	t ₆ – t ₇	t ₇ – t ₈																								
Input	:	1	1	1	0	1	0	1																								
Output	:	0	1	0	0	1	0	0																								
