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Sixth Semester B.E./B.Tech. Degree Examination, Dec.2024/Jan.2025

Signals and Digital Signal Processing

Time: 3 hrs.

Max. Marks: 100

Note: Answer any FIVE full questions, choosing ONE full question from each module.

Module-1

- 1 a. For the following discrete time systems, determine whether the system is : i) Linear
ii) Time invariant iii) Memory less iv) Causal v) Stable.
I) $y(n) = x(1-n)$ II) $y(n) = \log_{10}(|x(n)|)$ (06 Marks)
- b. Sketch the even and odd component of the continuous time signal $x(t)$ shown in Fig.Q.1(b) (06 Marks)

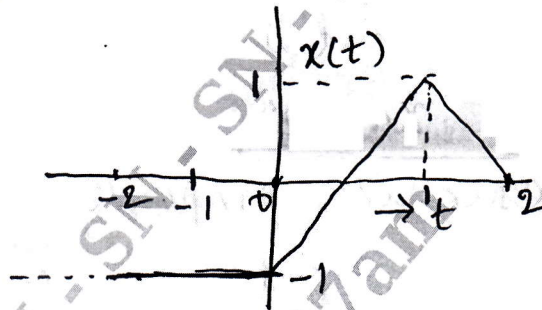


Fig.Q.1(b)

- c. Consider an LTI system with unit impulse response $h(t) = u(-t + 2)$. If the input applied to the system is $x(t) = u(t + 2) - u(t - 1)$ find the output $y(t)$ of the system. (08 Marks)

OR

- 2 a. Consider an LTI system with input $x(n) = 2^n u(-n)$ and impulse response $h(n) = u(n)$. Compute the output of the system $y(n)$ and also plot it. (10 Marks)
- b. Check whether the following discrete time signals are energy or power signals:
i) $x(n) = \begin{cases} 3(-1)^n; & n \geq 0 \\ 0; & n < 0 \end{cases}$ ii) $x(n) = A\delta(n)$ (06 Marks)
- c. Find the step response for the LTI system represented by $h(t) = e^{-|t|}$. (04 Marks)

Module-2

- 3 a. Let $x[n]$ be a finite length sequence with $X(K) = \{10, -2 + j2, -2, -2 - j2\}$. Using the properties of DFT find the DFT^s of the following sequences i) $x_1(n) = x((n + 2))_4$
ii) $x_2(n) = x(4 - n)$. (08 Marks)
- b. Prove the periodic property of DFT. (02 Marks)
- c. Using overlap save method, compute $y(n)$ of a FIR filter with impulse response $h(n) = \{3, 2, 1\}$ and input $x(n) = \{2, 1, -1, -2, -3, 5, 6, -1, 2, 0, 2, 1\}$ (10 Marks)

OR

- 4 a. Using frequency domain approach, compute the energy of the 4 point sequence

$$x(n) = \sin\left(\frac{2\pi}{N}n\right), 0 \leq n \leq 3$$
 (08 Marks)
- b. State and prove the following properties of DFT i) Time reversal ii) Circular convolution iii) Multiplication. (12 Marks)

Module-3

- 5 a. Develop an 8-point decimation in frequency FFT algorithm. Draw the complete signal flow graph. (10 Marks)
- b. Find 4 point circular convolution of $x(n)$ and $h(n)$ using radix-2 DIF-FFT algorithm.
 $x(n) = \{1, 1, 1, 1\}$, $h(n) = \{1, 0, 1, 0\}$. (10 Marks)

OR

- 6 a. First five points of 8-point DFT of a real valued sequence is given by $x(k) = \{0, 2 + j2, -j4, 2 - j2, 0\}$; Determine the remaining points. Hence find the sequence $x(n)$ using DIF-FFT algorithm. (10 Marks)
- b. Why FFT is needed? Explain the classification of FFT algorithms. (05 Marks)
- c. List any two similarities and differences between DIT and DIF algorithms. (05 Marks)

Module-4

- 7 a. Design a chebyshev analog filter with ripple of 0.5dB in the passband $|\Omega| \leq 1$ and at $\Omega = 3$, amplitude is down by 3dB. (10 Marks)
- b. Obtain $H(z)$ using impulse invariance method for following analog filter.

$$H_a(s) = \frac{1}{(s + 0.5)(s^2 + 0.5s + 2)}$$
 (10 Marks)

OR

- 8 a. Explain the frequency transformation in analog filters. (06 Marks)
- b. List the advantages and disadvantages of digital filter. (04 Marks)
- c. Design a unit band width 3dB digital Butterworth filter of first order by using bilinear transformation. (10 Marks)

Module-5

- 9 a. Obtain the direct form – I, direct form – II, cascade and parallel form realization for the following system $y(n) = 0.75y(n-1) - 0.125y(n-2) + 6x(n) + 7x(n-1) + x(n-2)$. (14 Marks)
- b. List the advantages and disadvantages of FIR filters. (06 Marks)

OR

- 10 a. Design the symmetric FIR lowpass filter whose desired frequency response is given as

$$H_2(\omega) = \begin{cases} e^{-j\omega t} & \text{for } |\omega| \leq \omega_c \\ 0 & \text{other wise} \end{cases}$$

 The length of the filter should be 7 and $\omega_c = 1$ rad/sample. Use rectangular window. (10 Marks)
- b. Realize the following system function in i) Direct form ii) Cascade form

$$H(z) = 1 + \frac{3}{4}z^{-1} + \frac{17}{8}z^{-2} + \frac{3}{4}z^{-3} + z^{-4}$$
 (10 Marks)
