

## Sixth Semester B.E. Degree Examination, June/July 2024

### Digital Signal Processing

Time: 3 hrs.

Max. Marks: 100

Note: Answer any FIVE full questions, choosing ONE full question from each module.

#### Module-1

- 1 a. Calculate 8-point DFT of  $x(n) = \cos\left(\frac{n\pi}{4}\right)$ . Draw magnitude and phase of  $x(k)$ . (10 Marks)
- b. Derive the DFT properties for Periodicity and linearity property. (10 Marks)

#### OR

- 2 a. Compute circular convolution of discrete sequence  $x_1(n) = \{1, 3, 5, 3\}$   $x_2(n) = \{2, 3, 1, 1\}$  by i) Circular method ii) Matrix method. (10 Marks)
- b. Find the output  $y(n)$  of a filter whose impulse response is  $h(n) = \{1, 1, 1\}$  and the input signal to the filter is  $x(n) = \{3, -1, 0, 1, 3, 2, 0, 1, 2, 1\}$ . Using overlap save method. (10 Marks)

#### Module-2

- 3 a. Develop an 8-point DIF-FFT algorithm starting from DFT. State clearly all the step. Explain how it reduces the number of computation. (10 Marks)
- b. Find DFT of  $x(n) = \{1, 1, 1, 1, 0, 0, 0, 0\}$  using DIT – FFT algorithm show all the intermediate result in signal flow graph. (10 Marks)

#### OR

- 4 a. The DFT  $x(k)$  of sequence is given as  $x(k) = \{0, 2, +2j, -j4, 2 -j2, 0, 2 +2j, j4, 2 -j2\}$  using using IDIF – FFT. Determine  $x(n)$ . (10 Marks)
- b. Develop an 8-point IDIT-FFT algorithm starting from DFT. Draw the complete signal flow graph to find  $x(n)$ . (10 Marks)

#### Module-3

- 5 a. Design an analog Butterfly filter has a gain – 2dB and 20r/s and attenuation in excess of 10dB beyond 30r/s. (10 Marks)
- b. Determine the transfer function if Chebyshev filter for the following specification :
  - i) Maximum passband reple is 1dB
  - ii) Stop and band attenuation is 40dB for  $\Omega \geq 4r/s$ . (10 Marks)

#### OR

- 6 a. For the constraints  $0.8 \leq |H(e^{jw})| \leq 1$  for  $0 \leq w \leq 0.2\pi$ ,  $|H(e^{jw})| \leq 0.2$  for  $0.6\pi \leq w \leq \pi$ . Design a Butterworth digital filter using bilinear transformation. Assume  $T = 1$  Second. (10 Marks)
- b. Using Impulse invariant technique find the transfer function of digital filter  $H(z)$  for analog Transform function

$$H(s) = \frac{b}{(s+a)^2 + b^2}$$

(10 Marks)

Important Note : 1. On completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages.  
2. Any revealing of identification, appeal to evaluator and /or equations written eg. 42+8 = 50, will be treated as malpractice.

**Module-4**

- 7 a. Design a Chebyshev filter with  $T = 1$  second using Bilinear transformation for the following specification.
- i)  $0.8 \leq |H(e^{jw})| \leq 1$  for  $0 \leq w \leq 0.2\pi$
  - ii)  $|H(e^{jw})| \leq 0.1$  for  $0.5\pi \leq w \leq \pi$  (10 Marks)
- b. Realise the system for direct Form – I and direct form – II.
- $$H(z) = \frac{0.7 - 0.25z^{-1} - z^{-2}}{1 + 0.1z^{-1} - 0.72z^{-2}} \quad (10 \text{ Marks})$$

**OR**

- 8 a. Obtain the parallel form and cascade form for given system.
- $$y(n) = 0.75 y(n-1) - 0.125y(n-2) + 6 x(n) + 7x(n-1) + x(n-2) \quad (10 \text{ Marks})$$
- b. Design a maximally flat digital LPF to meet following specification.
- $$0.8 \leq |H(e^{jw})| \leq 1 \text{ for } 0 \leq w \leq \pi/4$$
- $$|H(e^{jw})| \leq 0.18 \text{ for } 0.75\pi \leq w \leq \pi$$
- Using impulse invariant transformation. Assume  $T = 1$  Sec. (10 Marks)

**Module-5**

- 9 a. For a given FIR filter  $y(n) = x(n) + 2/5 x(n-1) + 3/4x(n-2) + \dots$ . Draw direct form – I and Lattice structure. (10 Marks)
- b. Design the symmetric FIR lowpass filter whose desired frequency response is given as
- $$H_d(w) = \begin{cases} e^{-jwz} & \text{for } |w| \leq w_c \\ 0 & \text{otherwise} \end{cases}$$
- The length of the filter should be 7 and  $w_c = 1$  radius/sample use rectangular window. (10 Marks)

**OR**

- 10 a. Determine the filter coefficient  $h_d(n)$  for the desired frequency response of a low pass filter given by
- $$H_d(e^{jw}) = \begin{cases} e^{-j2w} & \text{for } -\frac{\pi}{4} \leq w \leq \frac{\pi}{4} \\ 0 & \text{for } \frac{\pi}{4} \leq |w| \leq \pi \end{cases}$$
- If we define the new filter coefficient by  $h(n) = h_d(n) \cdot w(n)$  where
- $$w(n) = \begin{cases} 1 & \text{for } 0 \leq n \leq 4 \\ 0 & \text{for otherwise} \end{cases}$$
- Determine  $h(n)$  and also the necessary response  $|H(e^{jw})|$  and compare with  $|H_d(e^{jw})|$  determine  $H(e^{jw})$  Determine  $H(e^{jw})$  using Hamming window. (10 Marks)
- b. Determine form structures of cascad first order section also as a cascade 1<sup>st</sup> and 2<sup>nd</sup> order section form FIR lattice filter for  $H(z) = (1 + 0.6z^{-1})^5$ . (10 Marks)

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