

## Sixth Semester B.E. Degree Examination, June/July 2024 Finite Element Method

Time: 3 hrs.

Max. Marks: 100

*Note: Answer any FIVE full questions, choosing ONE full question from each module.*

### Module-1

- 1
  - a. State and explain the principle of minimum potential energy. (04 Marks)
  - b. Write short notes on plane stress and plane strain with stress-strain relation. (06 Marks)
  - c. Find the displacement at the mid point of a bar shown in FigQ1 (c), using Rayleigh Ritz method. Given  $E = 70 \times 10^3 \text{ MPa}$ ,  $A = 100 \text{ mm}^2$ . Use 2<sup>nd</sup> order polynomial displacement model. (10 Marks)

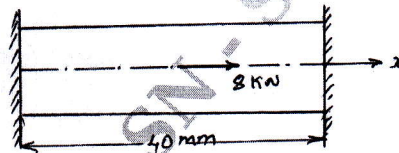


Fig. Q1 (c)

### OR

- 2
  - a. Determine the displacement at node 1 and 2 in the spring system shown in Fig. Q2 (a) by using principle of minimum Energy. (10 Marks)

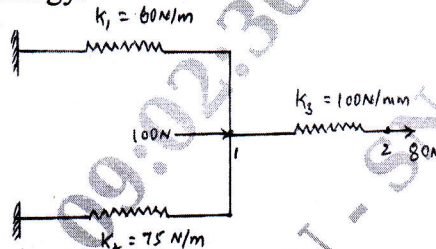


Fig. Q2 (a)

- b. What are convergence requirement? Discuss the condition of convergence requirement. Also define confirming and non conforming elements. (10 Marks)

### Module-2

- 3
  - a. Derive the elemental stiffness matrix for truss element. (10 Marks)
  - b. For the axially loaded bar shown in Fig. Q3 (b). Determine nodal displacement and stress in each element. Given  $E_{\text{steel}} = 2 \times 10^5 \text{ MPa}$ ,  $E_{\text{cu}} = 1 \times 10^5 \text{ MPa}$

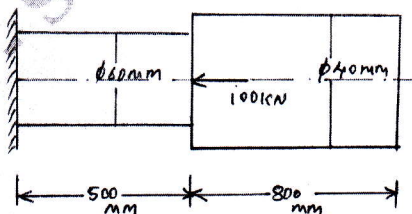


Fig. Q3 (b)

(10 Marks)

OR

- 4 a. Derive the Hermite shape function of the beam element and also show their variation. (10 Marks)
- b. For truss shown in Fig. Q4 (b), determine the nodal displacement and stresses in each element. Given  $E = 2 \times 10^5 \text{ N/mm}^2$ ,  $A_c = 200 \text{ mm}^2$

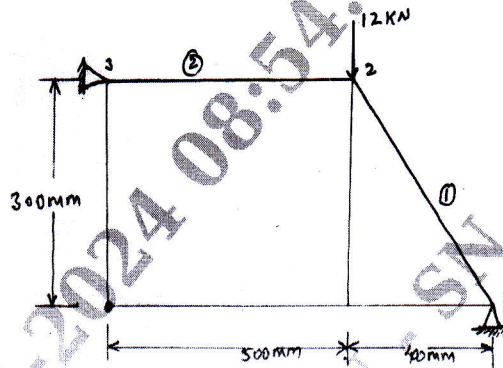


Fig. Q4 (b)

(10 Marks)

**Module-3**

- 5 a. Derive the shape function for CST element and show other variation. (10 Marks)
- b. For the triangular element shown in Fig. Q5 (b). Determine Jacobian matrix and also shape function at points  $P(3.85, 4.8)$  (10 Marks)

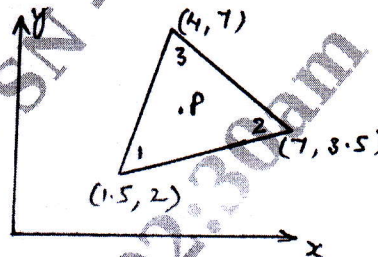


Fig. Q5 (b)

OR

- 6 a. Derive the expression for Jacobian matrix [J], displacement matrix [B] and stiffness matrix [K] for CST element. (15 Marks)
- b. List the difference between CST and LST elements. (05 Marks)

**Module-4**

- 7 a. What are isoparametric, subparametric and super parametric elements? Explain with neat sketches. (08 Marks)
- b. Explain 3 phases in FEA. (08 Marks)
- c. Mention the different commercially available software used for FEA. (04 Marks)

OR

- 8 a. What are axisymmetric elements? Explain the axisymmetric triangular element with neat sketches. (08 Marks)
- b. Derive the strain-displacement matrix for triangular element in the axisymmetric body. (12 Marks)



**Module-5**

- 9 a. Derive the Elemental stiffness matrix for heat conduction in 1D element. (08 Marks)  
 b. Find the temperature distribution in the 1D fin shown in Fig. Q9 (b).

$$T_{\infty} = 50^{\circ}\text{C}$$

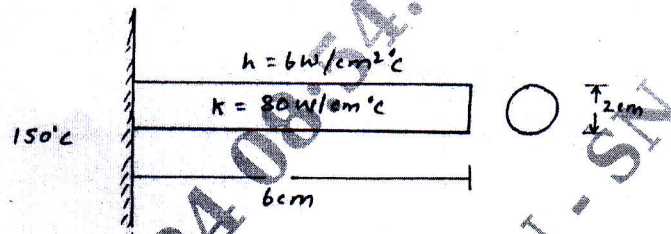


Fig. Q9 (b)

(12 Marks)

**OR**

- 10 a. State and explain the Hamilton's principle. Illustrate with example. (12 Marks)  
 b. Derive the expression for 1-D Element mass matrices. (08 Marks)

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