

# CBCS SCHEME

USN

18AS/AE63

## Sixth Semester B.E. Degree Examination, Jan./Feb. 2023

### Finite Element Method

Time: 3 hrs.

Max. Marks: 100

**Note:** Answer any FIVE full questions, choosing ONE full question from each module.

#### Module-1

1. a. Explain the principle of minimum potential energy, with the help of a continuum. (10 Marks)
- b. A fixed beam subjected to a point load at its centre using R-R method. Derive an equation for maximum deflection.

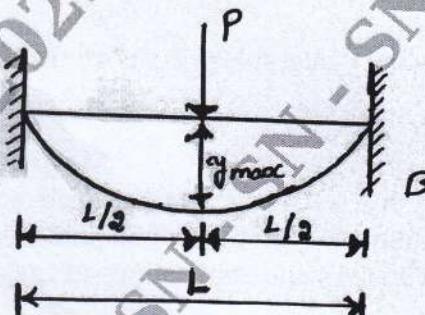


Fig Q1(b)

(10 Marks)

**OR**

2. a. Derive a relation between Cartesian Co-ordinate and natural co-ordinate system. (08 Marks)
- b. A simply supported beam is subjected to UDL, determine the max deflection using Galerkin's method.

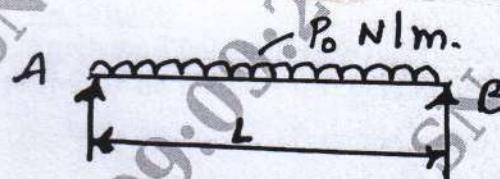


Fig Q2(b)

(12 Marks)

#### Module-2

3. a. Derive the shape function for a 1D bar element in natural co-ordinate system, also show the variation of shape function. (10 Marks)
- b. A compound bar is loaded as shown in Fig Q3(b)  $E_{Steel} = 200\text{GPa}$ ,  $E_{CU} = 100\text{GPa}$ , using elimination method of boundary condition, find
  - i) Nodal displacement
  - ii) Stresses in each element

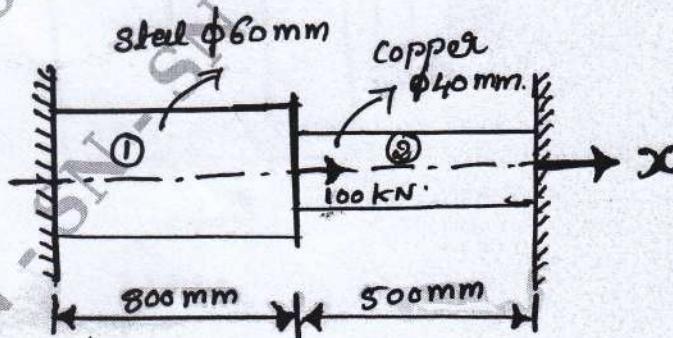


Fig Q3(b)

(10 Marks)

Important Note : 1. On completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages.  
2. Any revealing of identification, appeal to evaluator and / or equations written eg,  $42+8 = 50$ , will be treated as malpractice.

**OR**

- 4 a. Derive the stiffness matrix of a truss element.  
b. Derive the shape function of Beam element.

(10 Marks)  
(10 Marks)**Module-3**

- 5 a. Derive the shape function of a CST element.  
b. Derive the shape function of a four noded Quadrilateral element.

(10 Marks)  
(10 Marks)**OR**

- 6 a. Using Lagrangian interpolation, derive the shape function for 8-Noded Hexahedron element [HEXA-8].  
b. Using Serendipity Interpolation, derive the shape function of 8-noded quadrilateral element.

(10 Marks)  
(10 Marks)**Module-4**

- 7 a. Explain ISO, sub and super parametric element.  
b. Explain preprocessor, processor and post processor in finite element analysis.  
c. Give the advantages and applications of finite elements method.

(06 Marks)  
(08 Marks)  
(06 Marks)**OR**

- 8 a. Formulate an axisymmetric element showing the potential energy functional and strains.  
b. Derive the shape function of axiysymmetric triangular element and also the strain matrix.

(06 Marks)  
(14 Marks)**Module-5**

- 9 a. Explain conduction, convection and Radiation.  
b. Derive the Differential, equation for an 3D – heat conduction.

(09 Marks)  
(11 Marks)**OR**

- 10 a. Derive the stiffness matrix for 1-D fin.  
b. Determine the temperature distribution in the composite wall using 1D heat elements.  
Given :  $K_1 = 25\text{W/m}^\circ\text{C}$ ,  $K_2 = 35\text{W/m}^\circ\text{C}$ ,  $K_3 = 55\text{W/m}^\circ\text{C}$ ,  $h = 30\text{W/m}^2\text{C}$ ,  $T_\infty = 900^\circ\text{C}$ ,  $A = \text{unit area}$ .

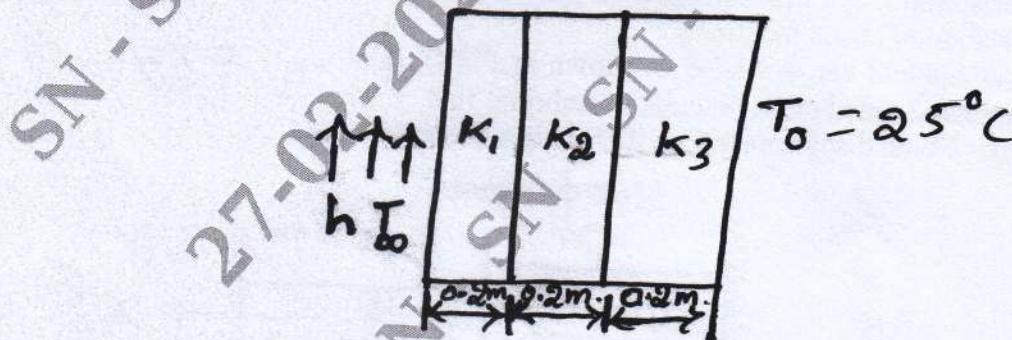


Fig Q10(b)

(12 Marks)

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