20MCM334

## Third Semester M.Tech. Degree Examination, Feb./Mar. 2022 **Operations Research**

Time: 3 hrs.

Max. Marks: 100

Note: Answer any FIVE full questions, choosing ONE full question from each module.

## Module-1

A Pension Fund Manager is considering investing in 2 shares A & B. It is estimated that 1

Share A will earn a dividend of 12% P.a and share B 4% P.a.

ii) Growth in the market value in one year of Share A will be 10 Paise per Re. 1 invested and in B, 40 Paise per Re. 1 invested.

He requires to invest the maximum total sum which will give

i) Dividend income of atleast Rs 600 per annum.

ii) Growth in one year of atleast Rs 1000 on the initial investment.

Formulate this problem as LP model to compute the minimum sum in order to be invested to meet the Manager's Objective. (10 Marks)

b. What are the application areas of Linear Programming?

(10 Marks)

Use Simplex method to solve 2

Max.  $Z = 3x_1 + 5x_2$ .

Subject to  $3x_1 + 2x_2 \le 18$ 

$$x_1 \le 4$$
 ;  $x_2 \le 6$  ;  $x_1, x_2 \ge 0$ .

Discuss the change in Cj on the Optimality of the optimal basic feasible solution. (12 Marks)

Explain the factors involved in Inventory Problem Analysis.

(08 Marks)

## Module-2

Solve by Graphical method: 3

Max.  $Z = 50x_1 + 30x_2$ 

Subject to 
$$2x_1 + x_2 \ge 18$$
  
 $x_1 + x_2 \ge 12$ 

$$3x_1 + 2x_2 \le 34$$

$$x_1, x_2 \ge 0.$$

(10 Marks)

Explain the Simplex Algorithm for maximization. Briefly explain all the steps involved. (10 Marks)

OR

Solve by Dual - Simplex method.

Max. 
$$Z = -3x_1 - 2x_2$$
  
Subject to  $x_1 + x_2 > 1$ 

Subject to 
$$x_1 + x_2 \ge 1$$

$$x_1 + x_2 \le 7$$

$$x_1 + 2x_2 \ge 10$$

$$x_2 \le 3$$
 ;  $x_1, x_2 \ge 0$ 

(10 Marks)

Consider the LPP

Max. 
$$Z = 3x_1 + 2x_2 + 5x_3$$

Subject to 
$$x_1 + 2x_2 + x_3 \le 430 + \lambda$$

$$3x_1 + 2x_3 \le 460 - 4 \lambda$$

$$x_1 + 4x_2 \le 420 - 4 \lambda$$

 $x_1, x_2, x_3 \ge 0$ . Find the critical range of  $\lambda$  for Optimal feasible solution. (10 Marks) 1 of 2

Module-3

Explain Kuhn - Tucker necessary and sufficient conditions in NLP.

(10 Marks)

Solve graphically

Max.  $Z = 2x_1 + 3x_2$ 

Subject to  $x_1^2 + x_2^2 \le 20$ 

$$x_1, x_2 \le 8$$
  
 $x_1, x_2 \ge 0$ .

(10 Marks)

What are the phases of Project Management? Explain with the help of a diagram. (10 Marks)

Explain different steps in Time Cost Trade - Off procedure.

(10 Marks)

**Module-4** 

A Supermarket has 2 sales girls at the sales counters. If the service time for each customer is exponential with a mean of 4 min. and if the people arrive in a Poisson fashion at the rate of 10 an hour, calculate i) Probability that a customer has to wait.

ii) Expected % of idle time for each sales girl.

iii) Expected length of waiting time.

(10 Marks)

Explain the reasons for carrying inventory.

(10 Marks)

OR

Explain Marginal Analysis approach in probabilitistic Inventory control models.

(10 Marks)

Explain necessary conditions for Optimality in Geometric programming.

(10 Marks)

Write a note on Terminology and Assumptions used in Sequencing models.

(10 Marks)

Use Dynamic programming to solve the following problem

Minimize  $Z = y_1^2 + y_2^2 + y_3^2$ .

Subject to 
$$y_1 + y_2 + y_3 \ge 15$$

$$y_1$$
,  $y_2$ ,  $y_3 \ge 0$ .

(10 Marks)

What are the types of Simulation? Briefly explain.

(10 Marks)

b. With the help of a block diagram, explain the steps in Simulation Process.

(10 Marks)