

## Sixth Semester B.E. Degree Examination, June/July 2024

### Signals and Digital Signal Processing

Time: 3 hrs.

Max. Marks: 100

**Note: Answer any FIVE full questions, choosing ONE full question from each module.**

#### Module-1

- 1 a. Distinguish between
- Continuous and Discrete time signal
  - Even and odd signal
  - Periodic and Non-periodic signal
  - Energy and power signal
- (08 Marks)
- b. Let  $y(t)$  and  $x(t)$  are given in Fig Q1(b). Sketch the following signal  $z(t) = x(2t) * y(1/2t + 1)$

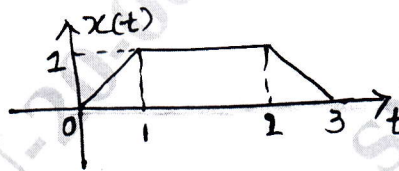


Fig Q1(b)

(06 Marks)

- c. Check whether the following signals are periodic or not. If periodic, find the fundamental period.
- $x_1(n) = \cos 2\pi n$
  - $x_2(t) = \cos 2\pi t \cdot \sin 4\pi t$
- (06 Marks)

**OR**

- 2 a. Determine whether the following signals are linear, time – invariant memory causal, stable.
- $y(n) = x(n^2)$
  - $y(t) = \frac{d}{dt}[e^{-t}x(t)]$
- (08 Marks)
- b. Evaluate the continuous time convolution integral given below :
- $$y(t) = e^{-2t}u(t) * u(t + 2)$$
- (06 Marks)
- c. Compute the convolution of the sequences.
- $$x(n) = \alpha^n u(n) ; y(n) = \beta^n u(n)$$
- When  $\alpha \neq \beta$  ; and  $\alpha = \beta$ .
- (06 Marks)

#### Module-2

- 3 a. Compute 4 point DFT of causal three samples sequence given by
- $$x(n) = \frac{1}{3} ; 0 \leq n \leq 2$$
- $$= 0 ; \text{ else}$$
- (06 Marks)
- b. Compute 6-point DFT of the sequence  $x(n) = [4, 3, 2, 1, 0, 0]$ . Also plot magnitude and phase spectrum.
- (08 Marks)
- c. Prove the following properties of DFT
- Linearity
  - Circular time shift.
- (06 Marks)

OR

- 4 a. Consider a FIR filter with impulse response  $h(n) = [3, 2, 1, 1]$  if the input is  $x(n) = [1, 2, 3, 3, 2, 1, -1, -2, -3, 5, 6, -1, 2, 0, 2, 1]$ . Find the output  $y(n)$ . Use overlap-add method, assuming the length of block is 7. (10 Marks)
- b. Find the IDFT of the given sequence  $x(k) = [3, 2 + j, 1, 2 - j]$ . (05 Marks)
- c. Perform circular convolution of  $x_1(n) = \{2, 1, 2, 1\}$  and  $x_2(n) = \{1, 2, 3, 4\}$  using circular shift method. (05 Marks)

**Module-3**

- 5 a. Develop decimation in time algorithm for finding FFT. Draw signal flow graph for  $N = 8$  for DT algorithm. (10 Marks)
- b. Find the 8-point DFT of the following sequence using radix – 2 DIF – FFT algorithm.  $x(n) = [2, 1, 2, 1]$ . (10 Marks)

OR

- 6 a. Tabulate the number of complex multiplications and complex additions required for the direct computation of DFT and FFT algorithm for  $N = 8, 16, 32$ . (08 Marks)
- b. Find the 8 – point DFT of the sequence  $x(n) = [1, 1, 1, 1, 0, 0, 0, 0]$  using DIT – FFT radix – 2 algorithm. Draw the signal flow graph. (12 Marks)

**Module-4**

- 7 a. Let  $H(s) = \frac{1}{s^2 + \sqrt{2}s + 1}$  represent the transfer function of a low-pass filter with a passband of 1 rad/sec. Use frequency transformation to find the transfer function of the following analog filters.
- A low pass filter with passband of 10 rad/sec
  - A high pass filter with cut-off frequency of 10 rad/sec. (06 Marks)
- b. Compare Butterworth and Chebyshev filter approximations. (04 Marks)
- c. Design a butterworth analog high pass filter that will meet the following specifications :
- Maximum passband attenuation = 2dB
  - Passband edge frequency = 200 rad/sec
  - Minimum stopband attenuation = 20dB
  - Stopband edge frequency = 100 rad/sec. (10 Marks)

OR

- 8 a. Transform  $H(s) = \frac{s+a}{(s+a)^2 + b^2}$  into digital filter using impulse invariant technique. (08 Marks)
- b. Design the digital filter using Chebyshev approximation and bilinear transformation to meet the following specifications. Passband ripple = 1dB, for  $0 \leq \omega \leq 0.15\pi$  stopband attenuation  $\geq 20\text{dB}$  for  $0.45\pi \leq \omega \leq \pi$ . (12 Marks)

**Module-5**

- 9 a. The desired frequency response of the lowpass filter is given by

$$H_d(e^{jw}) = H_d(w) = \begin{cases} e^{-j3w} & ; \quad |w| < 3\pi/4 \\ 0 & ; \quad 3\pi/4 < |w| < \pi \end{cases}$$

Determine the frequency response of FIR filter if the hamming window is used, with  $N = 7$ .

(10 Marks)

- b. Design an ideal band pass filter with frequency response

$$H_d(e^{jw}) = 1, \text{ for } \pi/4 \leq |w| \leq 3\pi/4. \text{ Use rectangular window with } N = 11 \text{ in the design.}$$

(10 Marks)

**OR**

- 10 a. Obtain the direct form – I and direct form – II, cascade and parallel realizations for the following system.

$$y(n) = 0.75 y(n-1) - 0.125y(n-2) + 6x(n) + 7x(n-1) + x(n-2)$$

(10 Marks)

- b. Given the FIR filter with following difference equation

$$y(n) = x(n) + \frac{3}{4}x(n-1) + \frac{17}{8}x(n-2) + \frac{3}{4}x(n-3) + x(n-4). \text{ Draw direct form – I and}$$

cascade form.

(06 Marks)

- c. Realize the linear phase filter with the impulse response.

$$h(n) = \delta(n) - \frac{1}{2}\delta(n-1) - \frac{1}{4}\delta(n-2) - \frac{1}{4}\delta(n-2) + \frac{1}{4}\delta(n-3) - \frac{1}{2}\delta(n-4) + \delta(n-5).$$

(04 Marks)

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