# First Semester M.Tech. Degree Examination, Dec.2019/Jan.2020 Digital Circuits and Logic Design

Time: 3 hrs.

Max. Marks: 100

Note: Answer any FIVE full questions, choosing ONE full question from each module.

### Module-1

a. Determine the function 'f' realized by the network shown in Fig. Q1 (a). Show the map.
(06 Marks)

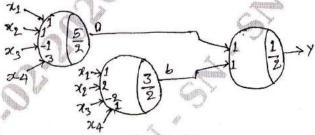


Fig. Q1 (a)

- b. Find the minimal and maximum true vertices of 'f' =  $x_1 x_2 + x_2 x_3 + x_1 x_3$ . (04 Marks)
- c. Consider the switching function 'f'.  $f(x_1, x_2, x_3, x_4) = \sum (3, 5, 7, 10, 12, 14, 15)$ . Find a minimal threshold logic realization. (10 Marks)

#### OR

2 a. Explain the capabilities of Threshold logic.

(04 Marks)

- b. Determine which of the following functions are unate or not:
  - (i)  $f_1(x_1, x_2, x_3, x_4) = \sum (1, 2, 3, 8, 9, 10, 11, 12, 14)$
  - (ii)  $f_2(x_1, x_2, x_3, x_4) = \sum (0, 8, 9, 10, 11, 12, 13, 14)$
  - (iii)  $f_3(x_1, x_2, x_3, x_4) = \sum (2, 3, 6, 10, 11, 12, 14, 15)$

(06 Marks)

- c. Determine the following functions are threshold or not:
  - (i)  $f_1(x_1, x_2, x_3) = \sum (0, 2, 4, 5, 6).$
  - (ii)  $f_2(x_1, x_2, x_3) = \sum (0, 3, 5, 6)$

If the given functions are threshold then write down the threshold gate.

(10 Marks)

## Module-2

- 3 a. For the circuit of Fig. Q3 (a),
  - (i) Find all the tests to detect input A' s-a-0 by using the sensitized path approach. (06 Marks)

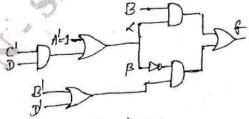
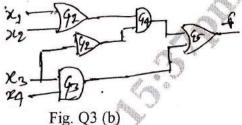


Fig. Q3 (a)

(ii) Show all the single faults that can be detected by the test (ABCD) = (1 1 1 1) (04 Marks)

b. For the circuit shown in Fig. Q3 (b), find all the tests to detect the faults  $x_3$ , s - a - 0 and  $x_3$ , s - a - 1.



orig. Q3 (

(10 Marks)

a. Use the map method to find a minimal set of tests for multiple faults for the 2-level AND-OR realization of the function,

$$f(w,x,y,z) = wz + xy + wx + wxy.$$

(10 Marks)

b. Use the map method to find a minimal set of sets for multiple faults for the 2-level OR-AND realization of the function,

$$f(w, x, y, z) = (w + \overline{x})(\overline{x} + \overline{z})(\overline{w} + y + \overline{z}).$$

(10 Marks)

Module-3

5 a. Explain the preset type of fault location experiment by considering the fault table as shown in Table Q5 (a). Write down corresponding (i) Reduced Table (ii) Fault dictionary. Also find out different sets of faults.

| 1              | $\mathbf{f}_{1}$ | $f_2$  | $f_3$ | f <sub>4</sub> | f <sub>5</sub> | f <sub>6</sub> |
|----------------|------------------|--|-------|----------------|----------------|----------------|
| $T_1$          |                  | The state of the s |       |                | 1              | 1              |
| T <sub>2</sub> | 1                |  | 1     |                | 1              |                |
| T <sub>3</sub> | lis.             |  |       | 1              | 1              | PHO.           |
| $T_4$          |                  | 1  | 1     |                | d              | 17             |
| T <sub>5</sub> | 1                |  |       | A              |                | 1              |
| T <sub>6</sub> | 1                |  | 1,4   |                | 3              | 1              |

Table Q5 (a)

(10 Marks)

b. Explain the adaptive four-level tree and adaptive three-level tree by considering T<sub>2</sub> & T<sub>6</sub> as initial test for the fault table shown in Table Q5 (b).

| Tests          | f <sub>0</sub> | fı   | $\mathbf{f}_2$ | $\mathbf{f}_3$ | f <sub>4</sub> | f <sub>5</sub> | f <sub>6</sub> | Output of fault free circuit |
|----------------|----------------|------|----------------|----------------|----------------|----------------|----------------|------------------------------|
| $T_1$          |                | - No |                |                |                | 1              | 1.             | 0                            |
| T <sub>2</sub> | 6              | 1    | 10000          | 1              |                | 1,             | Egilionei<br>C | » 1                          |
| T <sub>3</sub> | All I          | th/  | //III-, I      |                | 1              | 10             | ŋŢ             | 0                            |
| T <sub>4</sub> | 1              |      | 1              | 1              |                | ф              |                | 1                            |
| T <sub>5</sub> | J*             | 1    | All market     |                | A              | -              | 1              | 0                            |
| T <sub>6</sub> |                | 1    |                | 1              | 1              |                | 1              | 1                            |

Table Q5 (b)

(10 Marks)

OR

a. Draw the merger graph and its minimal form for the machine shown in Fig. Q6 (a).

(10 Marks)

| PS | NS, Z |                |                |                |  |  |
|----|-------|----------------|----------------|----------------|--|--|
|    | $I_1$ | I <sub>2</sub> | I <sub>3</sub> | I <sub>4</sub> |  |  |
| Α  | -     | C, 1           | E, 1           | B, 1           |  |  |
| В  | E, 0  | -              | -              | -              |  |  |
| С  | F, 0  | F, 1           | _              | _              |  |  |
| D  | -     | _              | B, 1           | _              |  |  |
| E  | -     | F, 0           | A, 0           | D, 1           |  |  |
| F  | C, 0  | _              | B, 0           | C, 1           |  |  |

Table Q6 (a)

2 of 4

b. Find the tests to detect the faults at  $x_3$ , s-a-0 and s-a-1 for the circuit shown in Fig. Q6 (b).

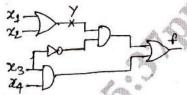


Fig. Q6 (b)

(10 Marks)

Module-4

7 a. For the machine in Table Q7 (a), determine the  $\pi$  – Lattice and basic partitions. Also show the derivation of the basic partitions.

| PS | NS    |                  |  |  |
|----|-------|------------------|--|--|
|    | x = 0 | x = 1            |  |  |
| A  | Е     | В                |  |  |
| В  | E     | Α                |  |  |
| C  | D     | $A_{\mathbb{R}}$ |  |  |
| D  | C     | F                |  |  |
| Е  | F     | (C)              |  |  |
| F  | Е     | C                |  |  |

Table Q7 (a)

(10 Marks)

- b. For the machine given in Table Q7 (b). Find
  - (i) Closed partitions.
  - (ii) Give the functional relationship based on the  $r_1 = \{\overline{A, B, C, D}; \overline{E, F, G, H}\}$ ,  $r_2 = \lambda_0 = \{\overline{A, C, E, G}; \overline{B, D, F, H}\}$ .
  - (iii) Write down the schematic diagram and  $\pi$ -Lattice for machine given in Table Q7 (b).

| PS     | N     | Z      |       |
|--------|-------|--------|-------|
|        | x = 0 | x = 1  |       |
| Α      | G     | D      | 1     |
| В      | H 4   | G<br>G | 0     |
| C      | F     | G      | 1     |
| D      | E     | G      | 0     |
| E      | C     | В      | 1     |
| F<br>G | C     | A      | × 0 * |
| G      | Α     | E      | 1     |
| Н      | В     | F(m)   | 0     |

Table Q7 (b)

(10 Marks)

8 a. For the machine shown in Table Q8 (a), find (i) π-Lattice and schematic diagram,
 (ii) Non trivial closed partitions, (iii) Parallel decomposition. (10 Marks)

| PS  | » NS  |       | Z |
|-----|-------|-------|---|
| A., | x = 0 | x = 1 |   |
| Α   | D     | G     | 0 |
| В   | С     | Е     | 0 |
| C   | Н     | F     | 0 |
| D   | F     | F     | 0 |
| E   | В     | В     | 0 |
| F   | G     | D     | 0 |
| G   | Α     | В     | 0 |
| Н   | Е     | С     | 1 |

Table Q8 (a)

b. Explain the decomposition of the composite machine with the help of possible realizations. Also brief the  $\pi$ -lattice of the composite machine. (10 Marks)

#### Module-5

9 a. What is an experiment? Explain the types of experiments.

(05 Marks)

b. Explain uncertainities by considering the machine shown in Table Q9 (b).

(05 Marks)

| PS | NS, Z |              |  |  |
|----|-------|--------------|--|--|
|    | x = 0 | x = 1        |  |  |
| A  | C, 0  | D, 1         |  |  |
| В  | C, 0  | <b>A</b> , 1 |  |  |
| С  | A, 1  | B, 0         |  |  |
| D  | B, 0  | C, 1         |  |  |

Table Q9 (b)

c. Explain and write down the successor tree for the machine M<sub>1</sub> shown in Table Q9 (c).

| PS | NS    | 5, Z  |
|----|-------|-------|
|    | x = 0 | x = 1 |
| Α  | C, 0  | D, 1  |
| В  | C, 0  | A, 1  |
| C  | A, 1  | B, 0  |
| D  | B, 0  | C, I  |

Table Q9 (c)

(10 Marks)

OR

a. Explain the Homing Experiment. Write down the Homing Tree for the machine M shown in Table Q10 (a). (10 Marks)

| PS | NS, Z |       |  |  |  |
|----|-------|-------|--|--|--|
| 4  | x = 0 | x = 1 |  |  |  |
| Α  | B, 0  | D, 0  |  |  |  |
| В  | A, 0  | B, 0  |  |  |  |
| C  | D, 1  | /A, 0 |  |  |  |
| D  | D, 1  | C, 0  |  |  |  |

Table Q10 (a)

b. (i) What is the main feature of the second algorithm for the design of Fault Detection experiments?

(ii) Write down the general procedure of the second algorithm.

(10 Marks)