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Fourth Semester B.E. Degree Examination, Jan./Feb. 2023

Design and Analysis of Algorithms

Time: 3 hrs.

Max. Marks: 100

Note: Answer any FIVE full questions, choosing ONE full question from each module.

Module-1

- 1
 - a. Explain the notion of algorithm. Design Euclid's algorithm for computing GCD (m, n). Find GCD (60, 24) using Euclid's algorithm. (08 Marks)
 - b. If $t_1(n) \in O(g_1(n))$ and $t_2(n) \in O(g_2(n))$, then prove that $t_1(n) + t_2(n) \in O(\max(g_1(n), g_2(n)))$. (08 Marks)
 - c. Distinguish between the two common ways to represent a graph. (04 Marks)

OR

- 2
 - a. Write an algorithm to find maximum of n elements and obtain its time complexity. (08 Marks)
 - b. Explain general plan of mathematical analysis of recursive algorithms with example. (08 Marks)
 - c. Explain the any four important problem types. (04 Marks)

Module-2

- 3
 - a. Write merge sort algorithm with example also calculate the efficiency. (12 Marks)
 - b. Discuss Strassen's matrix multiplication. (08 Marks)

OR

- 4
 - a. Write Quick sort algorithm with example. Also calculate the efficiency. (12 Marks)
 - b. Discuss topological sorting. (08 Marks)

Module-3

- 5
 - a. Explain Greedy Knapsack problem with example. (06 Marks)
 - b. Write an algorithm for minimum spanning tree using Kruskal's. (08 Marks)
 - c. Explain Heap sort technique. (06 Marks)

OR

- 6
 - a. Explain Coin change problem with example. (06 Marks)
 - b. Write an algorithm for minimum spanning tree using Prim's. (08 Marks)
 - c. Explain Huffman coding concept. (06 Marks)

Module-4

- 7
 - a. Explain transitive closure of a directed graph and find the transitive closure for the given graph.

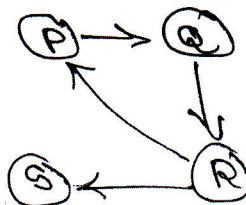


Fig Q7(a)

(10 Marks)

- b. Construct the optimal binary search tree for the following data :

| Key | A | B | C | D |
|-------------|-----|-----|-----|-----|
| Probability | 0.1 | 0.2 | 0.4 | 0.3 |

(10 Marks)

OR

- 8 a. Solve the following travelling sales person problem using dynamic programming technique.

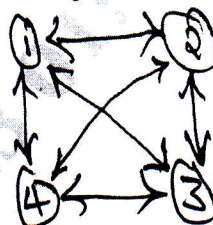


Fig Q8(a)

(10 Marks)

- b. Consider the following instance to solve the Knapsack problem using dynamic programming.

| Item | Weight | Value |
|------|--------|-------|
| 1 | 2 | \$12 |
| 2 | 1 | \$10 |
| 3 | 3 | \$20 |
| 4 | 2 | \$15 |

 $W = 5$

(10 Marks)

Module-5

- 9 a. Explain N-Queen problem with example. (08 Marks)
 b. Solve the following assignment problem using branch and bound technique.

| | job1 | job2 | job3 | job4 | |
|-------|------|------|------|------|----------|
| $C =$ | 9 | 2 | 7 | 8 | Person a |
| | 6 | 4 | 3 | 7 | Person b |
| | 5 | 8 | 1 | 8 | Person c |
| | 7 | 6 | 9 | 4 | Person d |

(12 Marks)

OR

- 10 a. Explain Hamiltonian cycles with example. (08 Marks)
 b. Solve the travelling sales person problem using branch and bound technique.

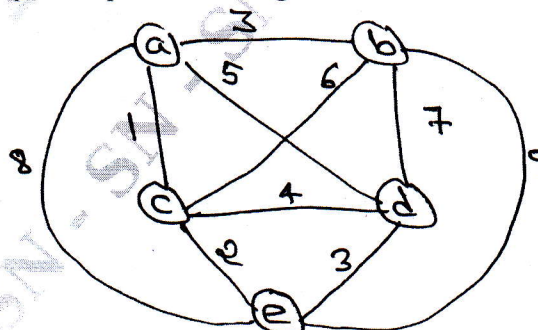


Fig Q10(b)

(12 Marks)
